## University of Saskatchewan Dept. of Electrical Engineering EE325 Communication Systems I

Midterm Examination - Friday, Feb. 19, 1999

1(a) Determine the normalized power and level in dBV for the following sinusoidal signals. Complete the following table using one decimal place accuracy. (2 points)

Signal	Level (dBV)	P norm (Watts)	(Revised Question				
700 mV rms @ 1000 Hz	-3	0.5					
10 volts rms @ 256 Hz	ညှိဝ	100	./ 7.571				
20 Vp-p sinusoid @ 60 Hz	17	50	20 Vp-p = 7.07 Vrms				
Sum of above 3 signals	<u> 21.8</u>	150.5	Sum power				
Checksum (of ali 4 rows)	55.8	301	(frequencies differ				

I(a) A modulator forms the product of the carrier signal  $c(t) = 100 \text{ V} \cos 2\pi 20000 \text{ t}$  and the following signals m(t). Determine the amplitudes and frequencies of the components in the modulated output signal. Assume single sided spectrum for your solution. (2 points)

m(t)	A (volts)	f <sub>l</sub> (kHz)	A2 (volts)	f <sub>2</sub> (kHz)	A3 (volts)	f3 (kH2)	A4 (volts)	f4 (kHz)
$2\cos 2\pi 4000t$	100	16	100	24				
$4\cos 2\pi 11000t$	200	9	200	31				
$2 + 6\cos 2\pi 23000t$	300	3	200	20	300	43		
$\cos 2\pi 4000t + \cos 2\pi 8000t$	50	12	50	16	50	24	50	28
Checksum	650	40	550	91	350	67	50	28



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i) Flat top sa

sampling? Explain v

ii) - a narrow This allows many (narrow) signals in a TOM multiplexer

- a flat top sample has a single value of waltage only one number needs to be stored in PCM of

- 2(b) In a digital transmission system, samples are placed in a digital latch as they arrive and the content of the latch remains until the next sample arrives. The latch is connected to an D/A convener which is followed by an analog lowpass filter.
  - (i) Does this system implement natural or flat top sampling? (1 point)
  - (ii) What is the duty cycle (in percent) of the decoded samples? (1 point)
    - i) Flat top sampling
    - ii) duty cycle is 100%.
- 2(c) A flat top sampled system has 50% duty cycle pulses prior to the 5 kHz lowpass reconstruction filter. Determine the output amplitude and frequency if the sampling rate is 10 kHz and the input modulation signal is 10 cos 2π4000t. (1 point)

$$\hat{W}(f) = \frac{\tau}{T} \frac{\sin \pi \tau f}{\pi \tau f} W(f)$$

$$\hat{W}(4RHz) = \frac{\tau}{T} \frac{\sin \pi \tau f(4000)}{\pi \tau (4000)} (10) \qquad T_s = \frac{1}{f_s} = 101$$

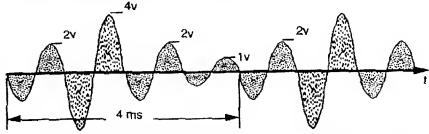
$$T = 0.5T_s = \frac{1}{f_s}$$

$$A = 4.68 \text{ Vp at } 4000 \text{ Hz}$$

15/02/20

A periodic waveform consists of four 1 ms segments each with one cycle of sinewave. The

sinewave amplitudes in the 4 successive segments are 2v, 4v, 2v, and 1v. The periodic waveform has a repetition rate of 250 Hz and has no discontinuities.



(a) Determine the normalized average power and peak to rms ratio of the waveform. (2 points)

$$\langle P_N \rangle = \frac{1}{4} \left( \frac{a^2}{2} + \frac{4^2}{2} + \frac{a^2}{2} + \frac{1^2}{2} \right) = \frac{1}{4} (12.5) = \boxed{3.125} \text{W}$$

$$V_{rms} = \sqrt{3.125} = 1.768 \text{V} \qquad V_p = 4 \text{V}$$

$$\frac{V_{peak}}{V_{rms}} = \boxed{2.263}$$

(b) The above waveform is quantized with an 11 bit encoder/decoder that has a range ±10.24 V. What is the SNR of the quantized waveform? Note that this question does not consider sampling. (2 points)

$$\frac{\text{Solution} \# 1}{\text{SNR}} - 5 = \frac{2(10.24 \text{V})}{2^{11}} = 10_{\text{mV}}, P_{\text{N}} = \frac{(10 \text{mV})^2}{12}$$

$$\frac{\text{SNR}}{(\text{dB})} = 10 \log_{10} \left(\frac{P_{\text{S}}}{P_{\text{N}}}\right) = 10 \log_{10} \left(\frac{3.125 \text{ W}}{8.33 \text{ WW}}\right) = \frac{55.74}{\text{dB}}$$

$$5NR = 5NR_{FLSW} + 10 \log_{10} \left( \frac{P_S}{P_{FLSW}} \right)$$

$$= 67.99 + (0 \log_{10} \left( \frac{3.125}{(10.24)^2/2} \right) = 55.74 dB,$$

$$10 \log_{10} \left( \frac{3.125}{(10.24)^2/2} \right) = 55.74 dB,$$

- 4. A 5 Vrms full load sinusoid with frequency 1000 Hz is to be quantized, coded and sent by digital transmission. Assume that the system bandwidth is 4 kHz and the sampling rate is 32 kilosamples per second (32 ks/s).
  - (a) What is the decoded SNR if 8 bit LPCM is used? (1 point)

$$5NR (dB) = 6.02(8) + 1.77 + 10 log_{10} \left(\frac{fs/2}{fbw}\right)$$

$$= 49.93 + 10 log_{10} \left(\frac{32000/2}{4000}\right) = [55.95dB]$$

(b) What is the decoded SNR if Delta Modulation is used? (1 point)

SNR = 
$$\frac{3f_s^2}{8\pi^2 f_m^2} \cdot \frac{f_s/2}{f_{bw}} = \frac{3(32000)^2}{8\pi^2 (1000)^2} \cdot \frac{16k}{4k} = 155.6$$
  
SNR (dB) = 10 log<sub>10</sub> 155.6 =  $21.92 dB$ 

(c) What is the decoded SNR if 4 bit linear DPCM is used? (1 point)

SNR (dB) = 
$$SNR_{AM} = 32ky + 20 \log_{10}(2^{4}-1)$$
  
=  $21.92 dB + 23.52 dB = 45.44 dB$ 

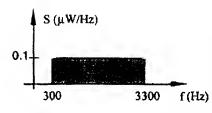
(d) What is the quantizing bin size (in volts) for the above three cases? (1 point)

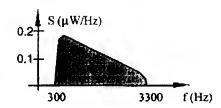
a) 
$$V_{rms} = 5V \Rightarrow V_{P-P} = 14.14v$$
  $S = \frac{14.14v}{2^8} = [55.2 \text{ mV}]$ 

b) Delta Mod. 
$$A_{max} W_m = 5f_5$$
  
at full Local  $S = 5\sqrt{2} \cdot 2\pi 1000 = 1.388V$ 

c) DPCM 
$$A_{mox} W_m = 5(2^{4}-1)f_5$$
 at full load  
 $5 = \frac{1388mV}{15} = 92.56 mV$ 

- 5(a) The (normalized) power spectral density of a voice signal and a 33.6 kb/s data signal are shown below.
  - Estimate normalized power and the level in dBV for each signal, (2 points)
  - Comment why one signal is easier to transmit using delta modulation (1 point)





i) 
$$P_N = (0.1 \text{ mW/H}_3)(3000 \text{ H}_3) = 300 \text{ M}$$

$$V_{rms} = \sqrt{300 \text{ mW}} = 17.3 \text{ mV}$$

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$$P_N = \left(\frac{0.18 + 0.02}{2}\right)(3000) = \boxed{300 \text{ aW}}$$

$$V_{rms} = \sqrt{300 \text{ aW}} = 17.3 \text{ mV}$$

ii) The voice signal will be less prone to slope overlow since the high frequencies have lower amplitude and this reduces the maximum rate of change i the signal. Step size can be smaller which yield higher SNR. (a) Assume a Mu Law encoder with minimum quantizing bin of 384 uV. Determine the 8 bit

codeword which best represents a voltage sample of +100 mV. (1 point)

Sample value = 
$$\frac{100 \text{ mV}}{384 \text{ mV}} = 260.4 \text{ units}$$

To find Mulaw mantissa 
$$260.4 = 2^4 (M+16.5)-16.5$$
 $M+16.5 = \frac{260.4+16}{2^4} = 17.3 \implies M=Round\{0.8\} = 1$ 

Sign = 0 (there is an error in the notes!)

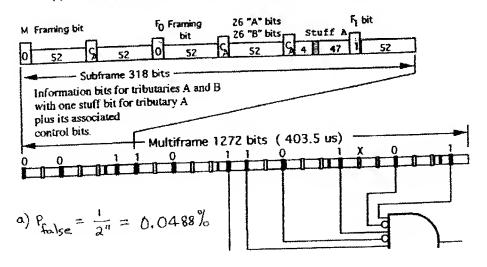
Result  $\Rightarrow$  [0 100 0001]  $\Rightarrow$  you can also look this up in the table.

The framing circuit in the receiver of a DSI-C transmission system observes 11 bits from 1272 bit history. Note that the X framing bit is not defined as "1" or "0". The observed bits are at the framing bit intervals illustrated in the frame illustration below. Assume tha the input (tributary) DS1 data bits are random.

Determine the probability of any specific sample of 11 data bits being mistaken for framing bits. (1 point)

Estimate the time required to find frame synchronization assuming that there are no channel errors (the true framing are always recognized when they are observed in the correct order by the detector) (2 points)

At what frequency do the stuff bits for channel A occur? (1 point)



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